



International Symposium  
Qualification of dynamic analyses of dams and their equipments  
and of probabilistic assessment seismic hazard in Europe  
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T. Tanaka

*President, The Japan Association of Rural Resource Recycling  
Solutions, Tokyo, Japan*

Session :

# ELASTO-PLASTIC DYNAMIC RESPONSE OF FILL-TYPE DAMS: TOTAL STRESS AND EFFECTIVE STRESS ANALYSES



Saint-Malo © Yannick LE GAL

# OUTLINE

## 1 INTRODUCTION

## 2 MATERIAL MODEL FOR CYCLIC BEHAVIOR OF SOIL

2.1 *Elasto-plastic model*

2.2 *Kinematic hardening model*

## 3 SHAKING TABLE TESTS OF EMBANKMENT DAMS AND DYNAMIC ANALYSES

3.1 *Outline of a model dam experiment*

3.2 *Dynamic analysis of embankment dam by simple constitutive model*

3.3 *Comparison of two and three dimensional dynamic analysis*

## 4 TOTAL STRESS ELASTO-PLASTIC DYNAMIC ANALYSIS

4.1 *Consolidated-undrained cyclic triaxial test*

## 5 OOGAKI DAM ELASTO-PLASTIC DYNAMIC ANALYSIS

5.1 *Oogaki Dam dynamic analysis by simple elasto-plastic model*

5.2 *Oogaki dam dynamic analysis by kinematic hardening elasto-plastic model*

## 6. SUMMARY

# INTRODUCTION

Simple strain softening material model for soil is used with the features of non-associated flow characteristics, post-peak strain softening, and strain-localization into a shear band. Then a kinematic hardening model considering the cumulative deformation by cyclic loading is developed based on the soil model of isotropic strain-hardening-softening property.

Total stress elasto-plastic constitutive model is rather simple and robust for application to a dynamic response analysis of fill-type dams. A cumulative damage concept for simple elasto-plastic model is effective by using the results of cyclic triaxial tests of saturated soils.

Dynamic progressive failure analysis of a small dry sand dam on shaking table is carried out. The computed acceleration and displacement at the crest of model dam is compared to the measured one. The computation of real fill-type dam is also carried out by total stress elasto-plastic model and effective stress constitutive model by taking into account the pore water build-up.

# YIELD & PLASTIC POTENTIAL FUNCTION

The yield function ( $f$ ) and the plastic potential function ( $\Phi$ ) are given by

$$f = \alpha I_1 + \frac{\bar{\sigma}}{g(\theta_L)} - K = 0$$

$$K = \frac{6c \cos \phi}{\sqrt{3}(3 - \sin \phi)}$$

$$\Phi = \alpha' I_1 + \bar{\sigma} - K = 0$$

$$\alpha = \frac{2 \sin \phi}{\sqrt{3}(3 - \sin \phi)}$$

$I_1$  : primary invariant of stress

$\bar{\sigma}$  : second invariant of deviatoric stress

# YIELD FUNCTION

In case of Mohr-Coulomb model,  $g(\theta_L)$  takes the following form

$$g(\theta) = \frac{3 - \sin \phi}{2\sqrt{3} \cos \theta - 2 \sin \theta \sin \phi}$$

$\phi$  : mobilized friction angle

$\theta$  : Lode angle (third invariant of deviatoric stress)

# SIMPLE STRAIN SOFTENING CONSTITUTIVE MODEL

Frictional softening is given by next function

$$\alpha(\kappa) = \alpha_p + \frac{\alpha_1 \kappa}{B + \kappa} \quad \alpha_1 = -(\alpha_p - \alpha_R)$$

Cohesion softening is given by next function.

$$K(\kappa) = K_p + \frac{K_1 \kappa}{D + \kappa} \quad K_1 = -(K_p - K_R)$$

Dilatancy is reduced by next equation

$$\alpha'(\kappa) = \alpha'_p \left(1 - \frac{\kappa}{C + \kappa}\right)$$

$\kappa$  is plastic parameter,  $B, C, D$  are constants for softening function

# ELASTIC PROPERTIES

Shear modulus  $G$  and damping ratio  $h$  are given by Hardin-Drnevich equation

$$G = \frac{G_0}{1 + \frac{\gamma}{\gamma_r}}$$

$$h = \frac{\frac{\gamma}{\gamma_r}}{1 + \frac{\gamma}{\gamma_r}} h_{\max}$$

$$G_0 = G_E \frac{(2.17 - e)^2}{1 + e} \sigma_m^{0.4}$$

$$K = \frac{2(1 + \nu)}{3(1 - 2\nu)} G$$

$\gamma$  is shear strain,  $\gamma_r$  is reference shear strain,  $\nu$  is Poisson's ratio,  $e$  is void ratio and,  $G_E$ ,  $h_{\max}$  are empirical constants

# FRictionAL HARDENING- SOFTENING FUNCTIONS

$$\alpha(\kappa) = \left( \frac{2\kappa^l \varepsilon_f^l}{\kappa^{2l} + \varepsilon_f^{2l}} \right)^m \alpha_p \quad (\kappa \leq \varepsilon_f) \quad \text{:hardening-regime}$$

$$\alpha(\kappa) = \alpha_r + (\alpha_p - \alpha_r) \exp \left\{ - \left( \frac{\kappa - \varepsilon_f}{\varepsilon_r} \right)^2 \right\} \quad (\kappa \geq \varepsilon_f) \quad \text{: softening-regime}$$

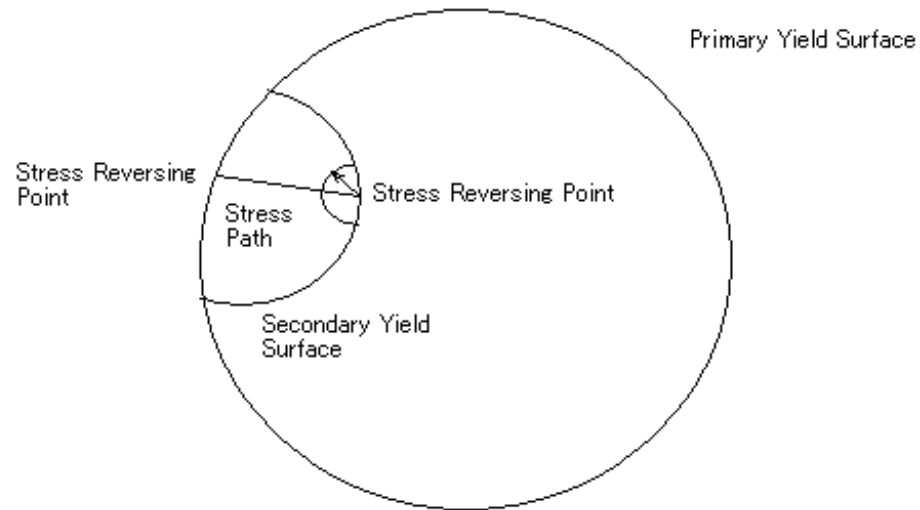
$$\phi_p \text{ (deg)} = \left\{ 59.47(1.5 - e) - 10(1 - e) \log \left\{ \frac{\sigma_3}{(\sigma_3)_0} \right\} \right\} g_R(\delta) \quad \text{: Tatsuoka et al.}$$

$$(\sigma_3)_0 = 4(1 - e) p_a \quad (p_a = 98 \text{ kPa})$$

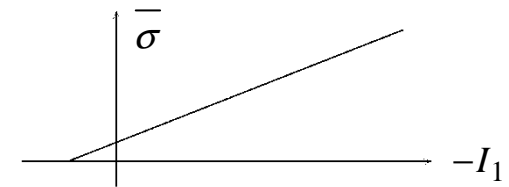
$$d\varepsilon_{ij} = d\varepsilon_{ij}^e + s d\varepsilon_{ij}^p \quad s = F_b / F_e \quad \text{: Shear band effect}$$



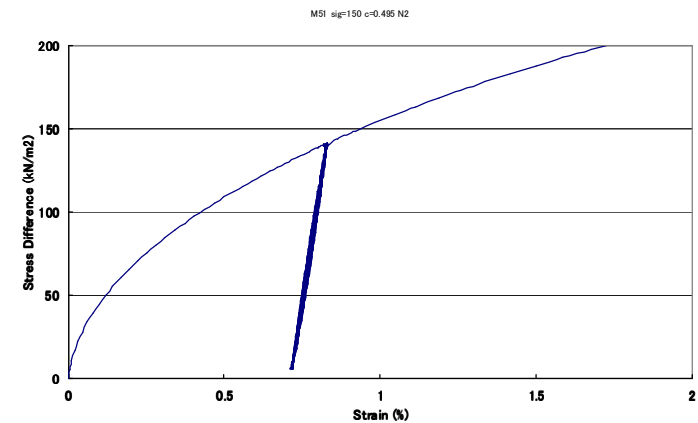
# KINEMATIC HARDENING CONSTITUTIVE MODEL ON $\pi$ PLANE



Mohr-Coulomb model takes pyramid shape



Upper part of  $-I_1$  and  $\bar{\sigma}$  relation



Calculated stress strain relation of triaxial test

# KINEMATIC HARDENING MODEL WITHIN BOUNDING SURFACE

$$\alpha_{iy}(\kappa') = \left( \frac{2\kappa'^l (\epsilon_f / a_f)^l}{\kappa'^{2l} + (\epsilon_f / a_f)^{2l}} \right)^m \alpha_p$$

$$\alpha(\kappa') = \alpha_{iy}(\kappa')(1 + e^n), \quad e = \eta / R$$

$$\alpha_{id}(\kappa') = \alpha - \alpha_p(e - 1.0) \quad e \geq 1.0$$

$$\alpha_{id}(\kappa') = \alpha \quad e < 1.0$$

$$\sin \psi' = \frac{3\sqrt{3}\alpha_{id}}{2 + \sqrt{3}\alpha_{id}}$$

# SOLUTION OF DYNAMIC ELASTO-PLASTIC FINITE ELEMENT ANALYSIS

## Element type

Very few element types can avoid the shear locking and dilatancy locking

One point integration of 4 nodes iso-parametric element with hour-glass control ( 8 nodes in three dimension element)

15 nodes triangular element (PLAXIS)

## Nonlinear solution method to avoid the accumulation of error

Dynamic equilibrium iteration is absolutely necessary (implicit method)

Return mapping method by explicit method is effective

## Strain softening with shear banding

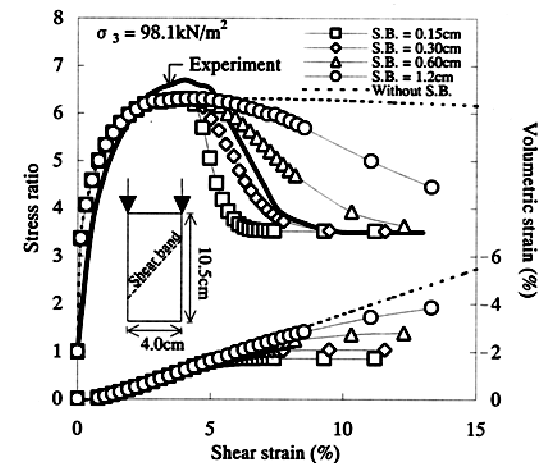
Objectivity of analysis (mesh independancy) : incorporating

a characteristics length of shear band in the material

modeling based on physical experimental observations

Simple check

Static 2D footing limit load analysis is a good benchmark regarding above remarks



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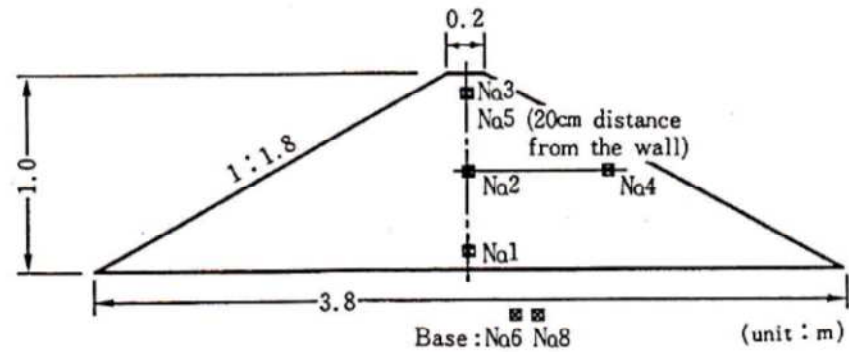
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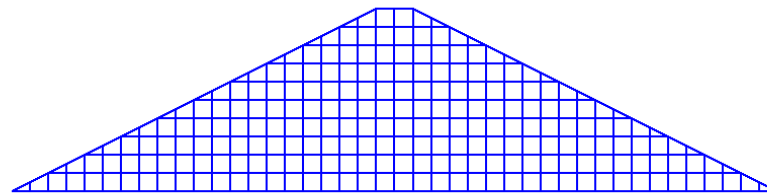
*5.2 Oogaki dam dynamic analysis by kinematic hardening elasto-plastic model*

## 6. SUMMARY

# EMBANKMENT DAM MODEL AND LOCATION OF ACCELEROMETERS

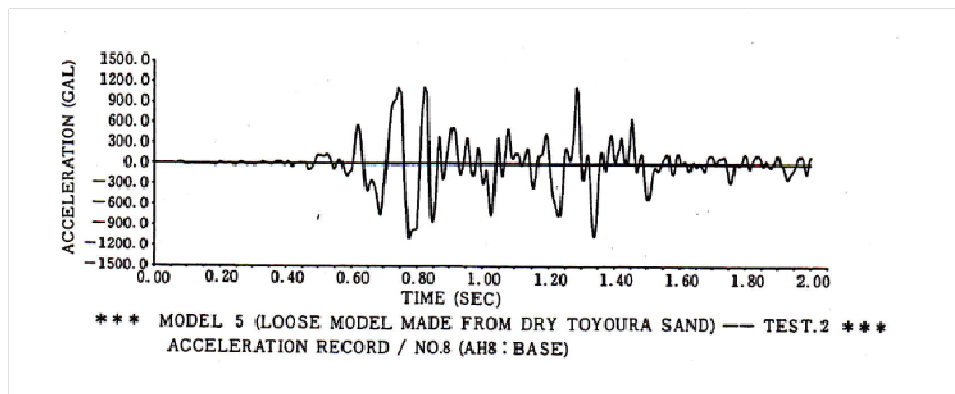


Embankment dam model and the location of accelerometers

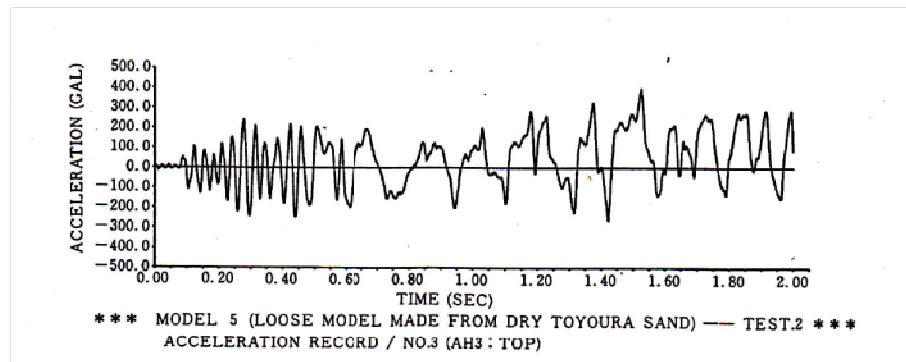


Finite element mesh used for the analysis

# OBSERVED ACCELERATION AT THE BASE AND CREST OF DAM MODEL



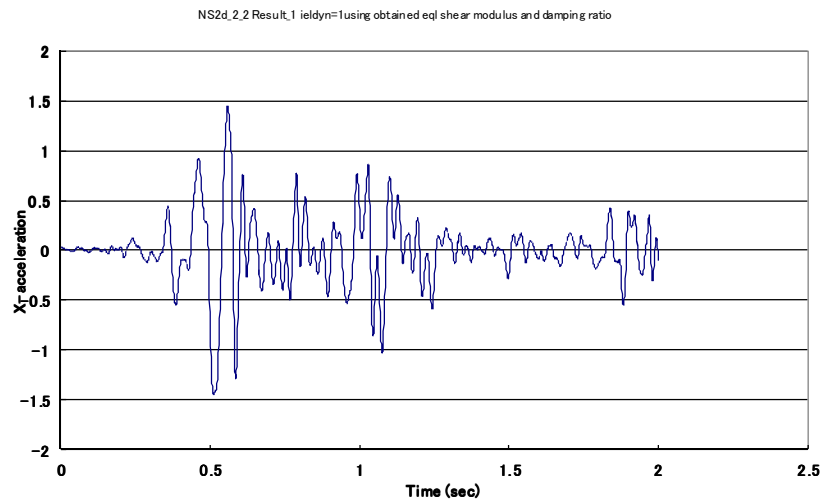
Input horizontal acceleration (observed at the base of shaking table)



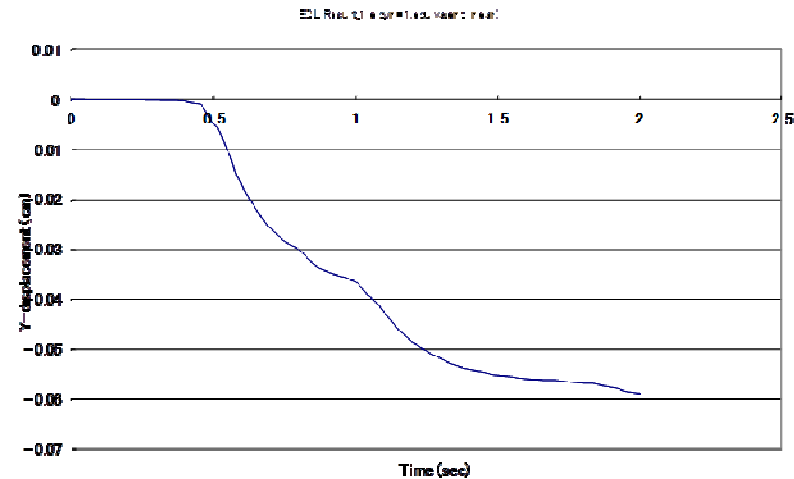
Observed acceleration at crest of the dam

# COMPUTED ACCELERATION AND SETTLEMENT (1)

Shear modulus and damping ratio are estimated by applying the equivalent linear method  
dry density =  $0.0014 \text{ kg/cm}^3$ ,  $\phi_P = 35^\circ$ ,  $\phi_R = 34^\circ$ ,  $G_E = 1200.0$ ,  $h_{\text{max}} = 0.25$ .



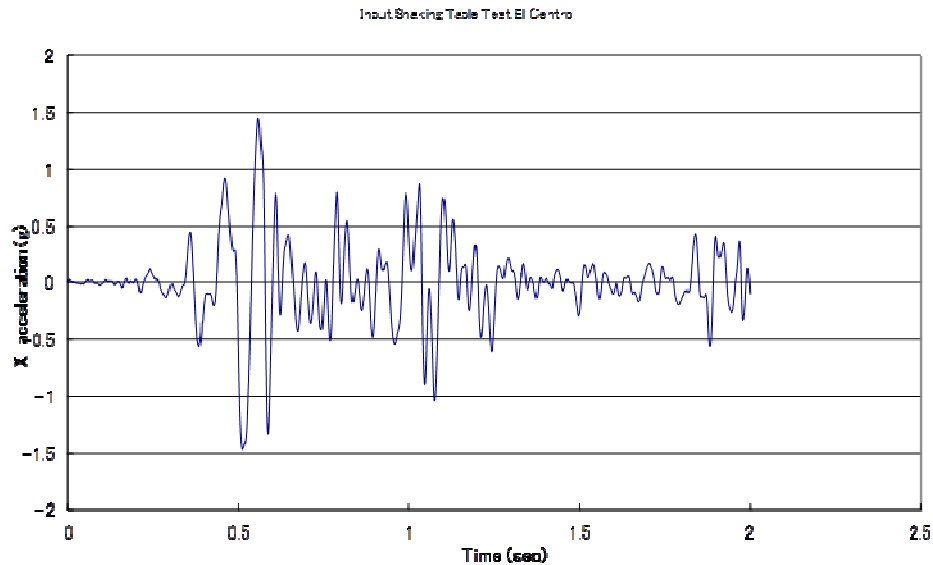
Computed horizontal acceleration at the center of dam crest



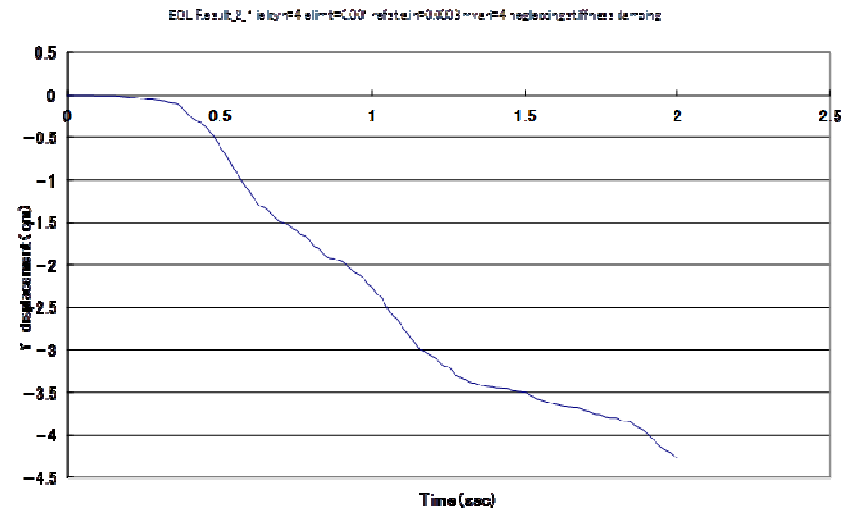
Computed settlement at the center of dam crest

# COMPUTED ACCELERATION AND SETTLEMENT (2)

## ELASTIC LIMIT=0.001



Computed acceleration at the center of dam crest (Rayleigh damping beta = 0)

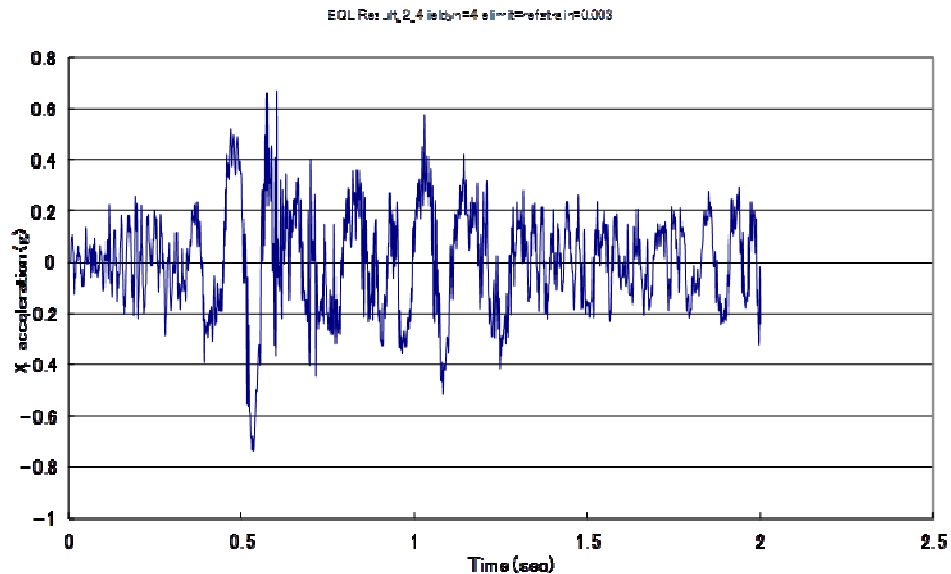


Computed settlement at the center of dam crest (Rayleigh damping beta = 0)

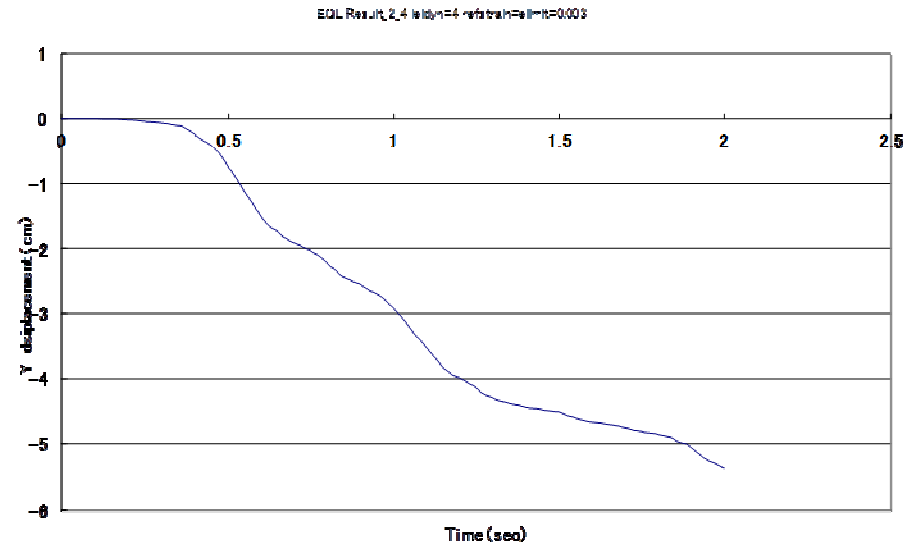


# COMPUTED ACCELERATION AND SETTLEMENT (3)

## ELASTIC LIMIT: reference shear strain for Hardin-Drnevich equation

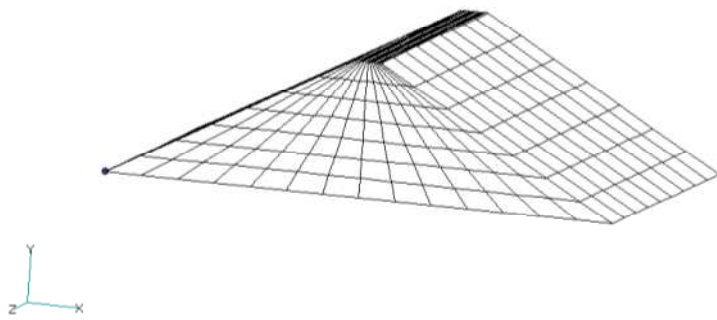


Computed acceleration at the center of dam crest.  
Rayleigh damping  $\beta = 0$ , elastic limit = 0.0003

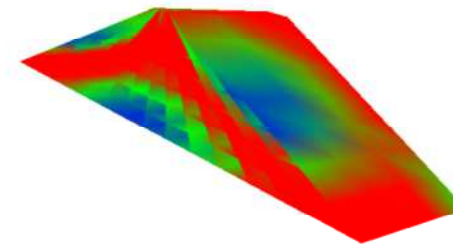
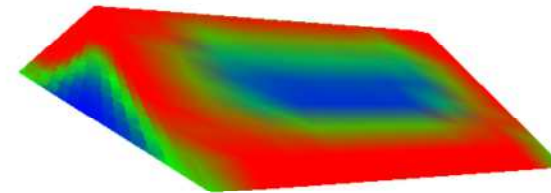


Computed settlement at the center of dam crest.  
Rayleigh damping  $\beta = 0$ , elastic limit = 0.0003

# THREE DIMENSIONAL FINITE ELEMENT ANALYSIS OF MODEL DAM ON SHAKING TABLE TEST



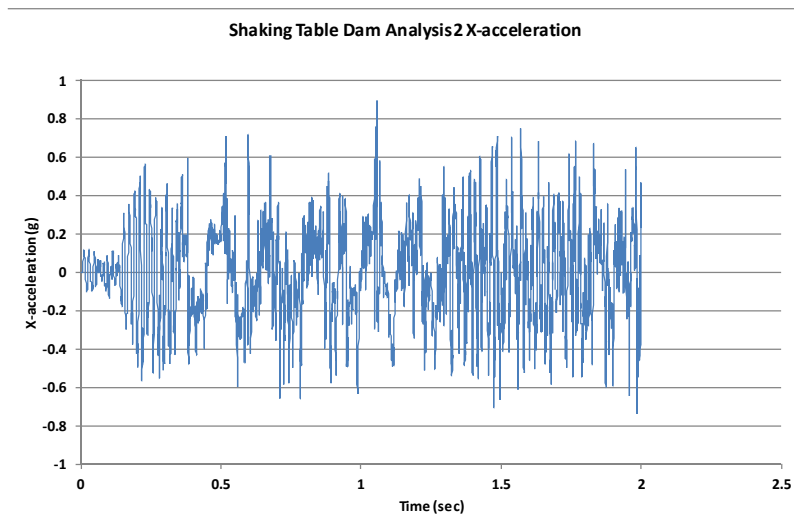
Three dimensional finite element mesh



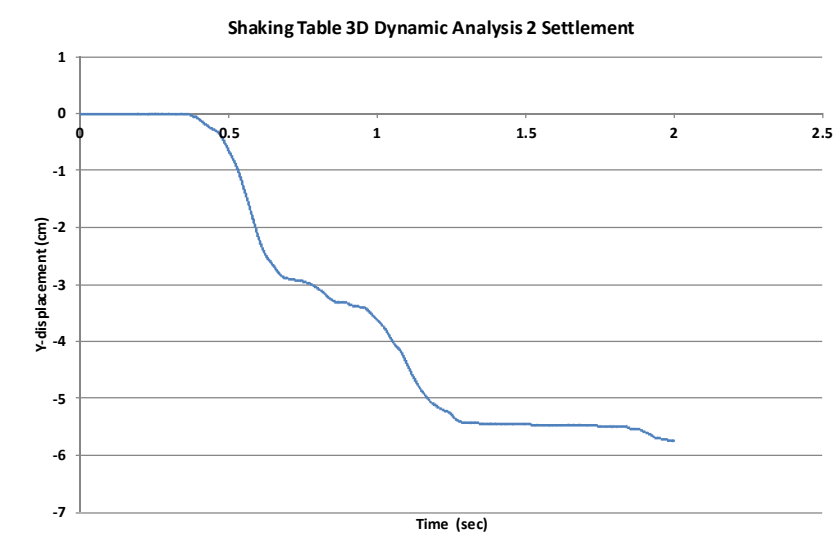
Peak maximum shear strain 29%

Computed maximum shear strain of model dam after shaking (peak strain 30%)

# COMPUTED HORIZONTAL ACCELERATION AND SETTLEMENT AT CREST OF MODEL DAM THREE DIMENSIONAL ANALYSIS

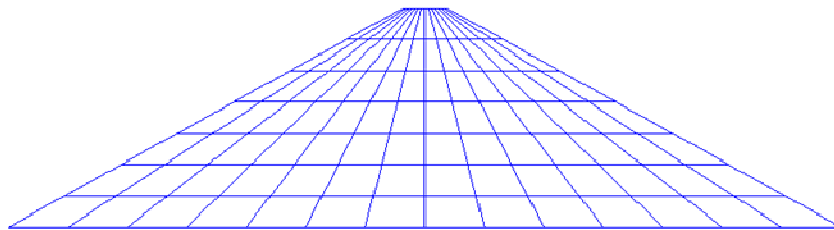


Computed horizontal acceleration at the crest of model dam

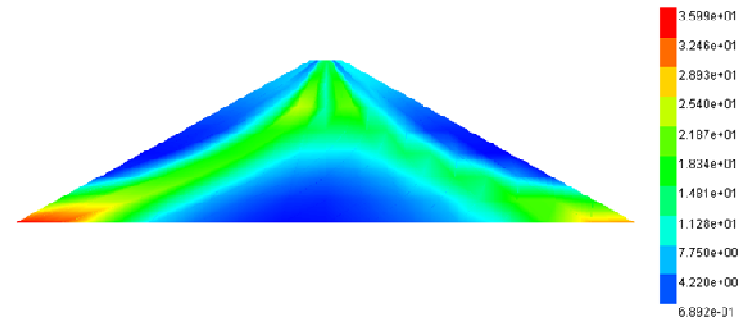


Computed settlement at the crest of model dam

# TWO DIMENSIONAL FINITE ELEMENT ANALYSIS OF MODEL DAM ON SHAKING TABLE TEST

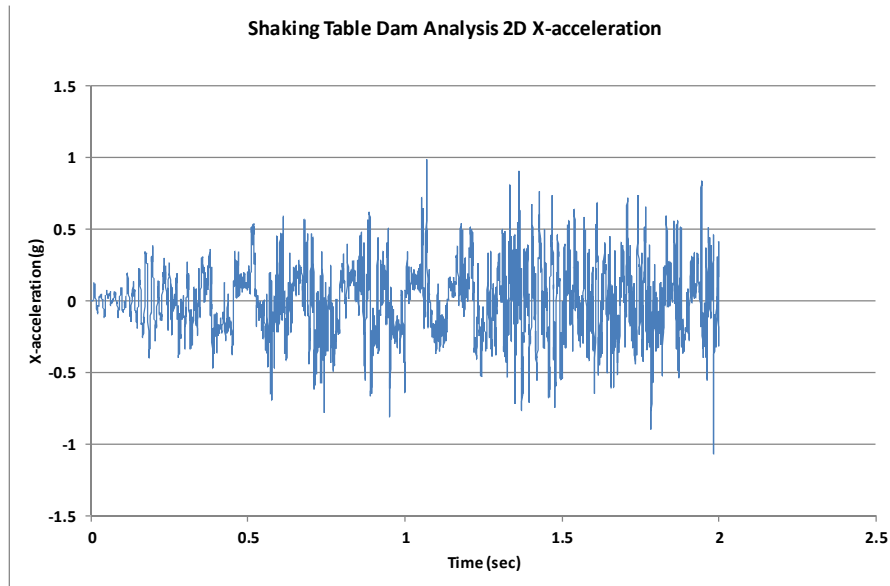


Two dimensional finite element mesh

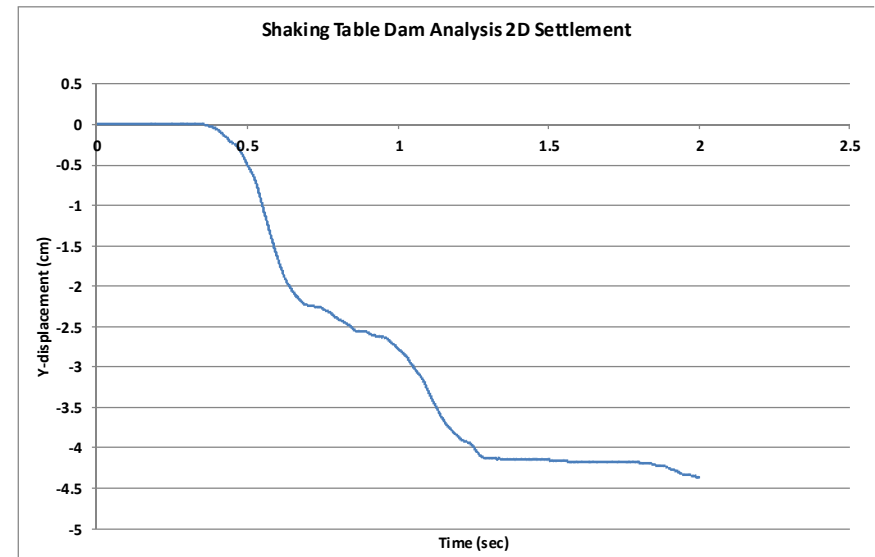


Computed maximum shear strain of model dam after shaking (peak strain 30%)

# COMPUTED HORIZONTAL ACCELERATION AND SETTLEMENT AT CREST OF MODEL DAM TWO DIMENSIONAL ANALYSIS

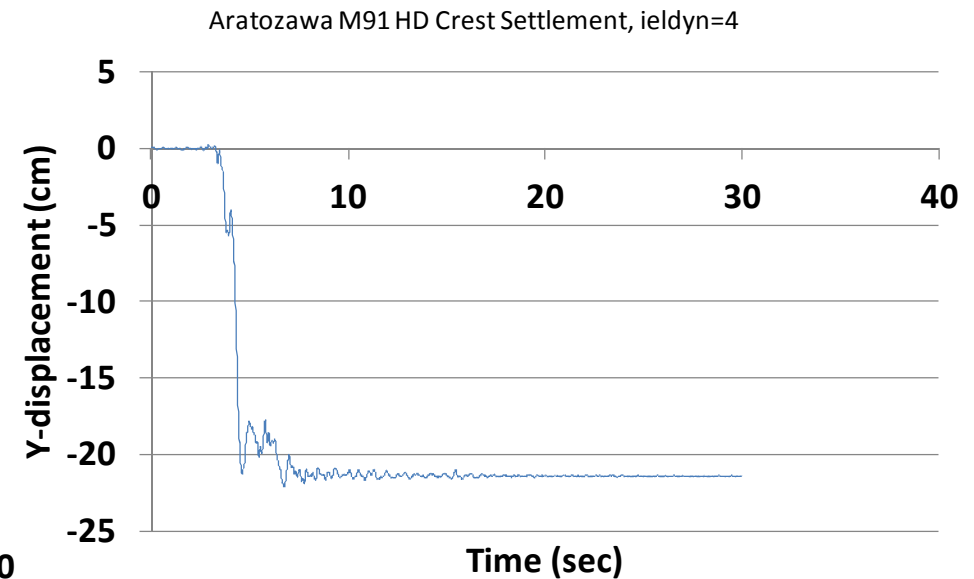
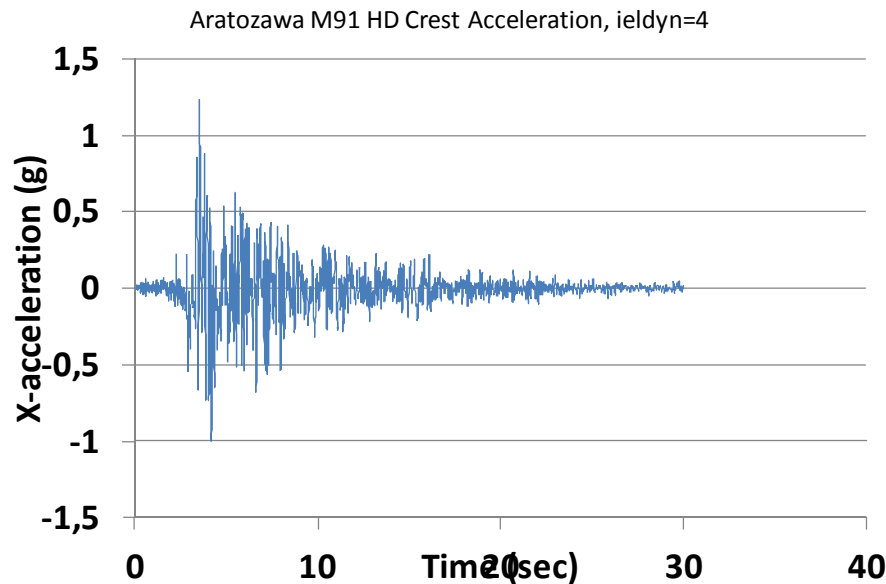


Computed horizontal acceleration at the crest of model dam



Computed settlement at the crest of model dam

# COMPUTED HORIZONTAL ACCELERATION AND SETTLEMENT AT CREST OF ARATOWAZAWA DAM TWO DIMENSIONAL ANALYSIS



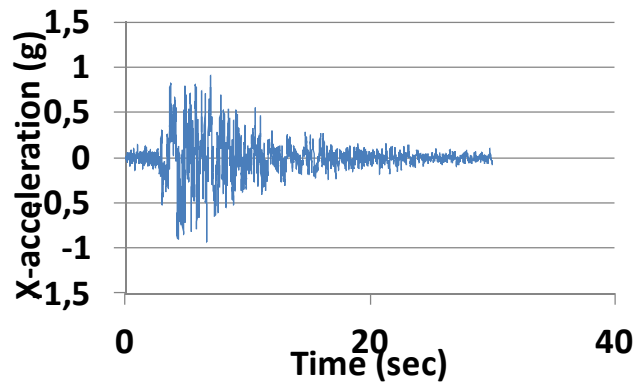
Computed horizontal acceleration at the crest of dam

Computed settlement at the crest of dam

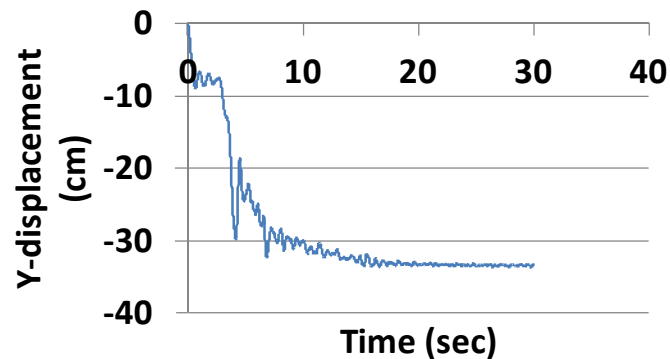
**Simple strain softening constitutive model (only peak strength, residual strength, shear band thickness & softening rate are needed)**

**Elastic limit for shear modulus and damping ratio : reference shear strain for Hardin-Drnevich equation**

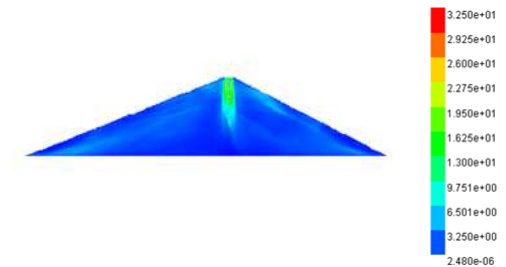
# COMPUTED HORIZONTAL ACCELERATION AND SETTLEMENT AT CREST OF ARATOZAWA DAM TWO DIMENSIONAL ANALYSIS



Computed horizontal acceleration at the crest of dam



Computed settlement at the crest of dam



Maximum shear strain distribution (%)

## Kinematic hardening constitutive model

Effective stress analysis: Core zone is undrained, Rock zones are drained

Elastic shear modulus and damping ratio \* 0.2 : reference shear strain for Hardin-Drnevich equation

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## 6. SUMMARY



# CNSOLIDATED-UNDRAINED CYCLIC TRIAXIAL TEST OF TRANSITION ZONE MATERIAL

- The advantage of the total stress analysis is that it is simple and numerically stable. The strength reduction in total stress is due to the plasticity or damage from a viewpoint of effective stress, cumulative shear strain that is similar to equivalent plastic parameter can be calculated in the elastic state.

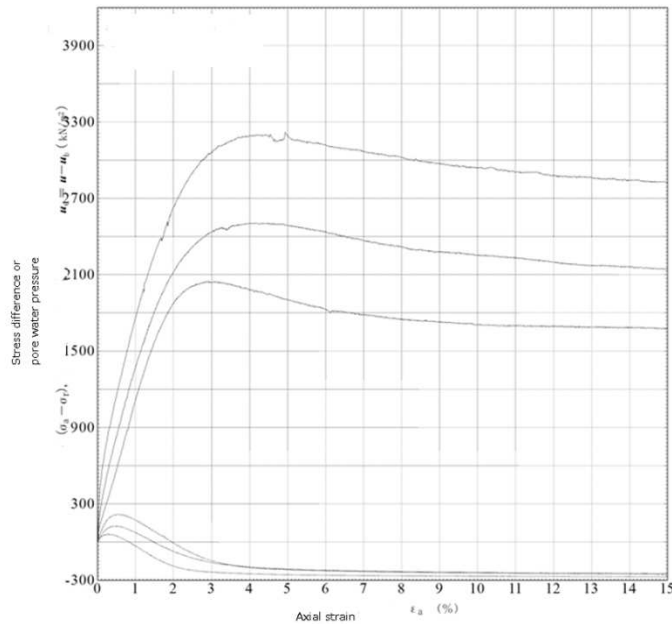
The integral of shear strain increments can be given by next equation.

$$\bar{\varepsilon} = \int d\bar{\varepsilon} \quad d\bar{\varepsilon} = (de_x^2 + de_y^2 + de_z^2) + 2de_{xy}^2$$

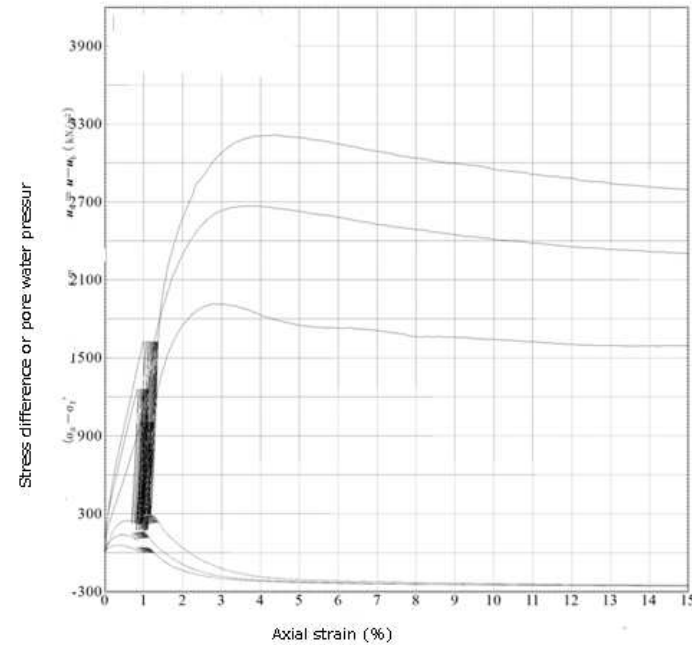
where  $de_x, de_y, de_z, de_{xy}$  are deviatoric components of strain.

- By applying empirical factor to this value by using the cyclic tri-axial test result, we can estimate the reduction of strength in total stress analysis. This process is similar to the damage concept of "simplified method by Tatsuoka et al."

# CONSOLIDATED UNDRAINED STRESS-STRAIN RELATION OOGAKI DAM ROCK MATERIAL (TRANSITION ZONE)



a)



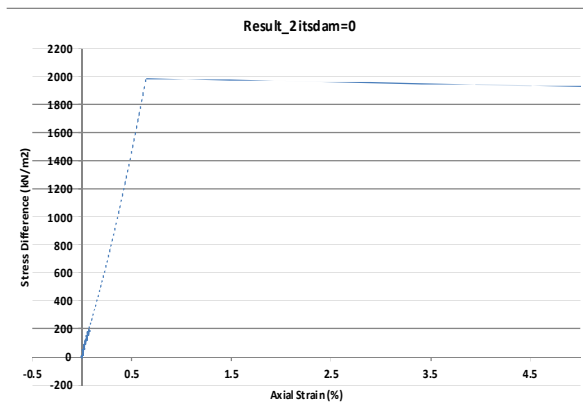
b)

Confining pressure: 200,400,600(  $\text{kN/m}^2$ )

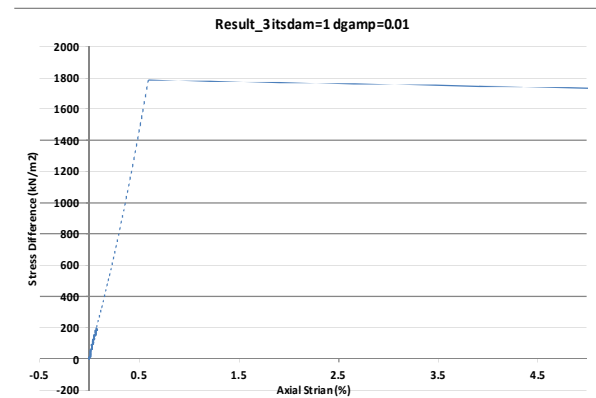
a) Monotonic loading

b) Cyclic and monotonic loading

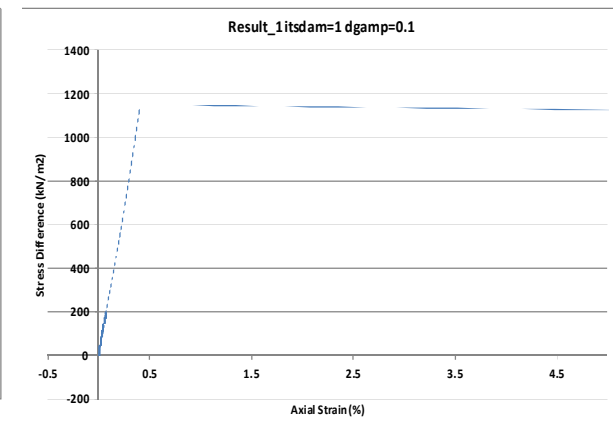
# COMPUTED STRESS-STRAIN RELATION BY SIMPLE CONSTITUTIVE MODEL



a)



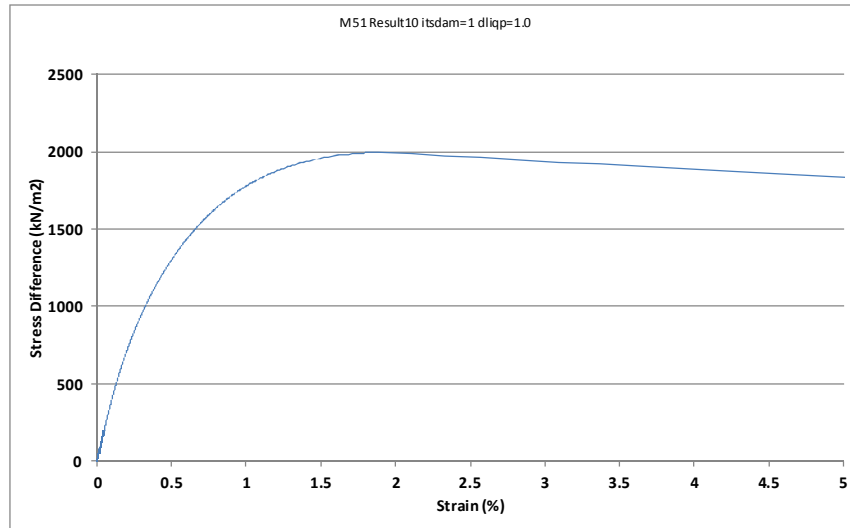
b)



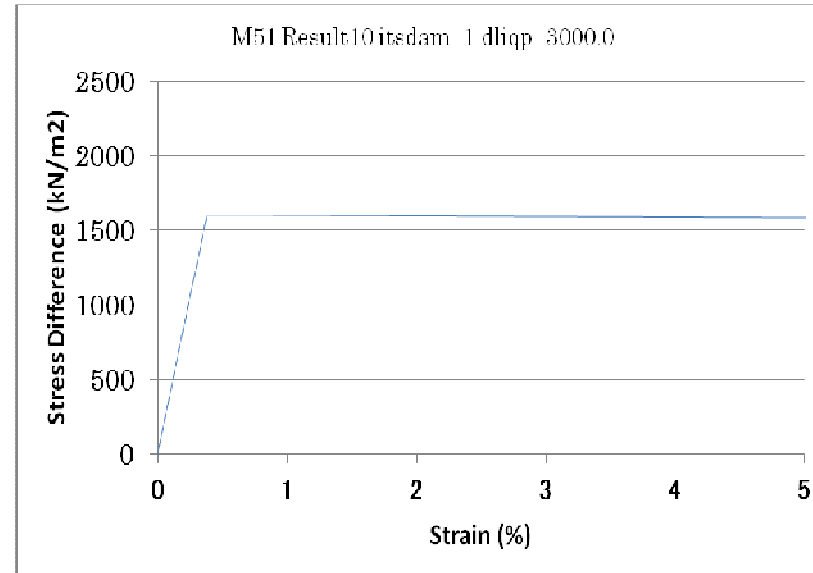
c)

Confining pressure is 200 (kN/m<sup>2</sup>) (applied cyclic load: 0 - 200kN/m<sup>2</sup>)  $\phi_p = 36.6^\circ$ ,  $\phi_r = 35.0^\circ$ ,  
 $B = 0.7$ ,  $C = 0.6$ ,  $D = 0.7$ , cohesion = 354 kPa,  
 a) without factor of equivalent plastic parameter , b) factor is 0.001, c) factor is 0.1

# COMPUTED STRESS-STRAIN RELATION BY KINEMATIC HARDENING ELASTO-PLASTIC MODEL



a)



b)

$$\phi_p = 36.6^\circ, \phi_r = 20.0^\circ, \varepsilon_f = 0.03, \varepsilon_r = 0.6, a_f = 5.0, m = 1, l = 0.5, n = 1.0, c = 374 \text{ kPa},$$

factor for plastic parameter  $\kappa'$  : a) = 1.0 , b) = 3000.0

In case b) stress-strain behavior is just similar to simple elasto-plastic strain softening model

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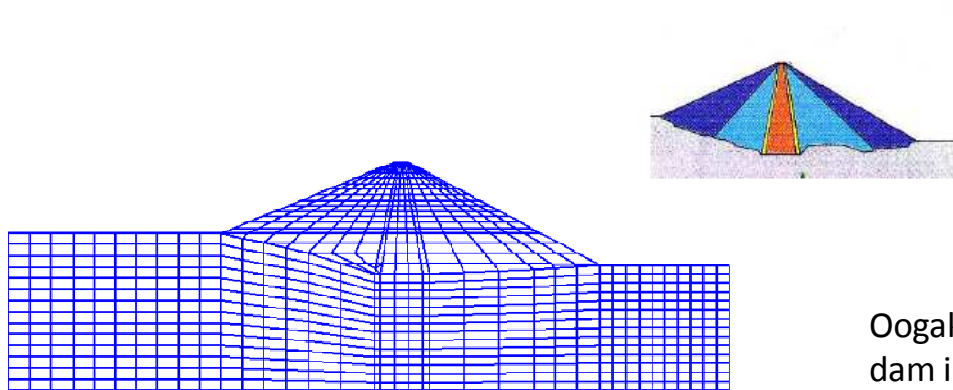
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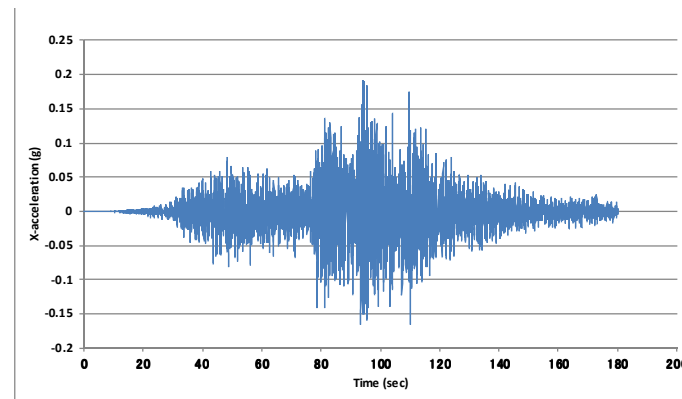
*5.2 Oogaki dam dynamic analysis by kinematic hardening elasto-plastic model*

## 6. SUMMARY

# OOGAKI DAM DYNAMIC ANALYSIS BY SIMPLE ELASTO-PLASTIC MODEL



Oogaki Dam finite element mesh. Height of this dam is 85.5 m. Blue shows transition zone



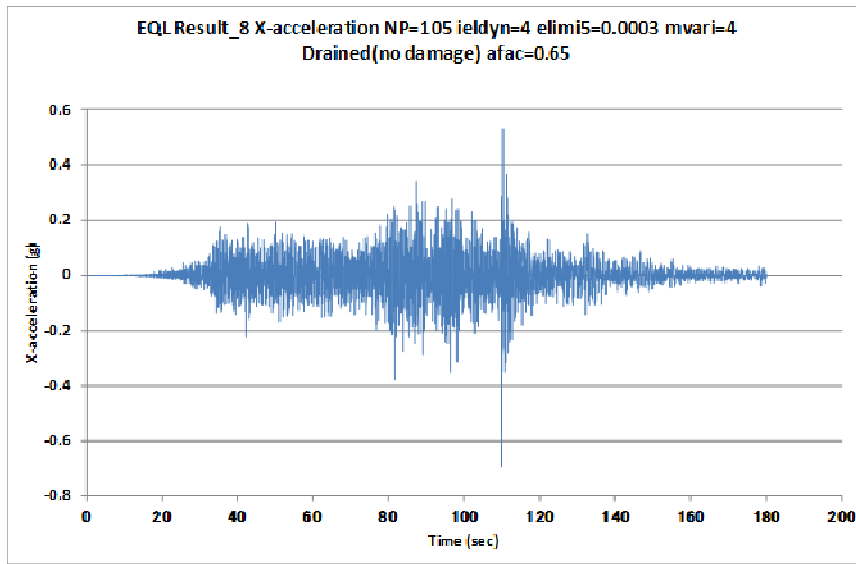
Estimated input acceleration at the base of the dam

# COMPUTED RESULTS BY SIMPLE CONSTITUTIVE MODEL TRANSITION ZONE IS DRAINED

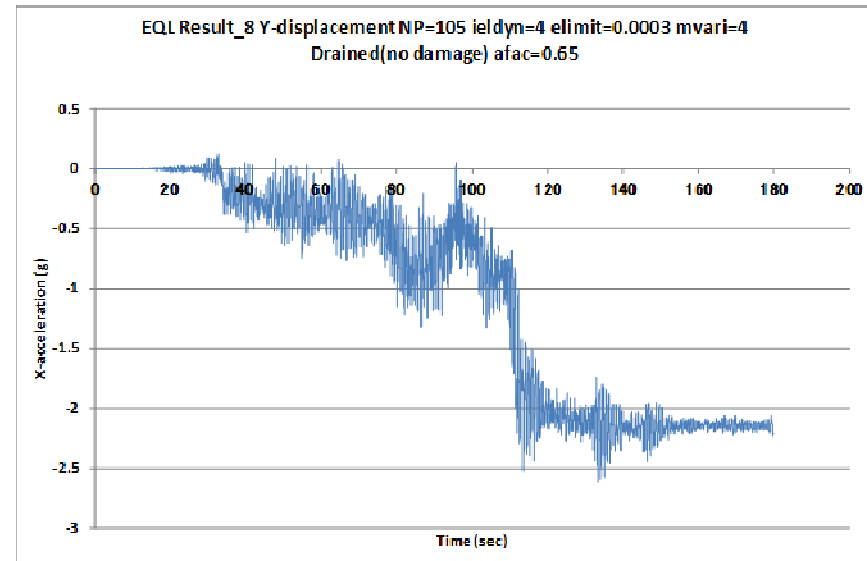
Core zone is undrained and another zones are completely drained

Transition zone material properties:

$\phi_p = 42.1^\circ$ ,  $\phi_r = 34.0^\circ$ ,  $B = 0.7$ ,  $C = 0.6$ ,  $D = 0.7$ , cohesion = 76 kPa, shear band thickness = 4 cm,  $G_E = 1200.0$ , Rayleigh damping alpha = 0, elastic limit = 0.0003.



Computed crest acceleration



Computed crest settlement

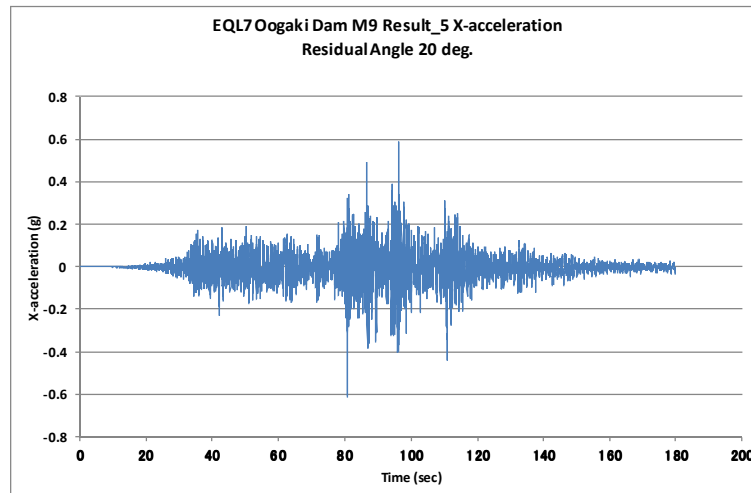
# COMPUTED RESULTS BY SIMPLE CONSTITUTIVE MODEL

## TRANSITION ZONE IS UNDRAINED

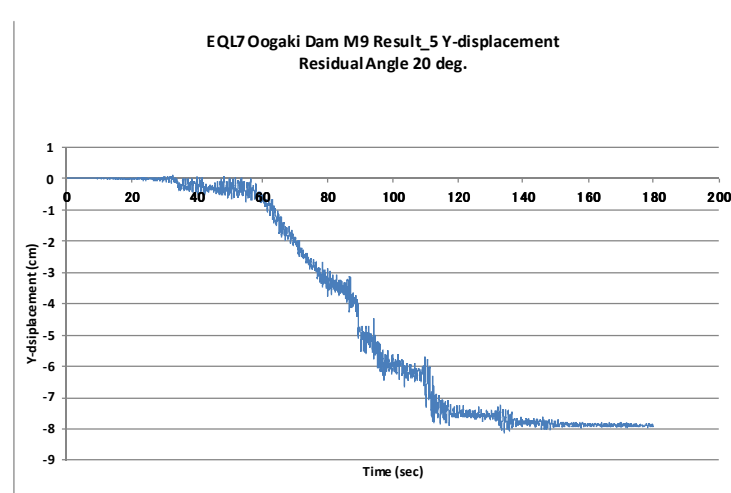
Core zone is undrained and another zones are completely drained

Transition zone material properties:

$\phi_p = 36.6^\circ$ ,  $\phi_r = 20.0^\circ$ ,  $B = 0.7$ ,  $C = 0.6$ ,  $D = 0.7$ , cohesion = 353 kPa, shear band thickness = 4 cm,  $G_E = 1200.0$ , Rayleigh damping alpha = 0, elastic limit = 0.0003.



Computed crest acceleration

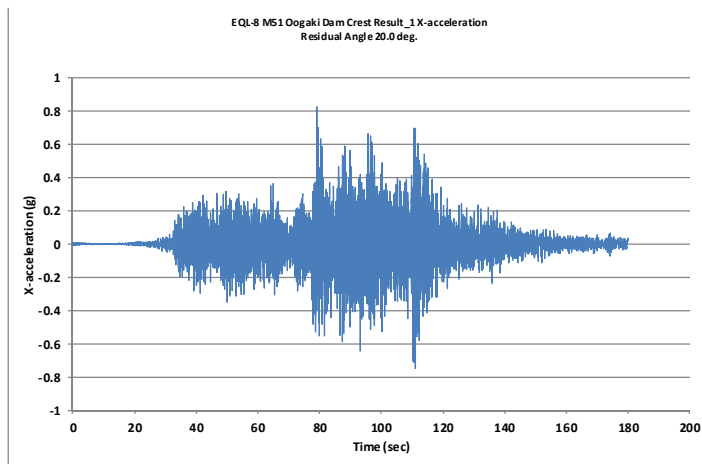


Computed crest settlement

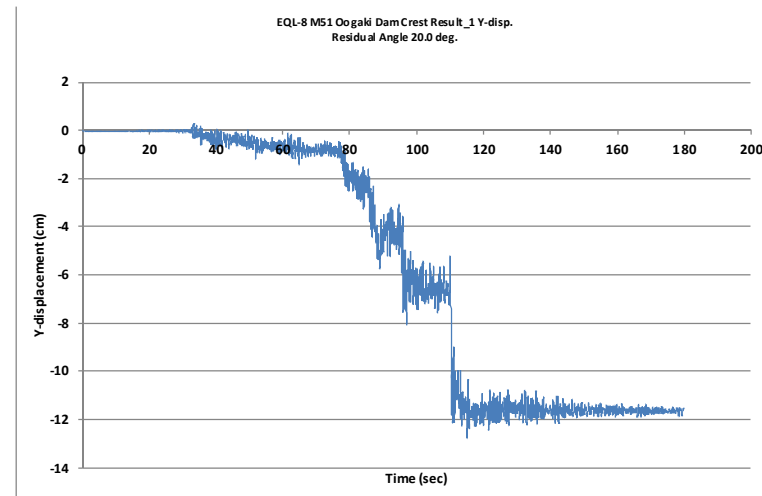


# DYNAMIC RESPONSE ANALYSIS BY KINEMATIC HARDENING ELASTO-PLASTIC MODEL (TOTAL STRESS ANALYSIS)

$c = 374 \text{ kPa}$ ,  $\phi_p = 36.6^\circ$ ,  $\phi_r = 20.0^\circ$ ,  $\varepsilon_f = 0.03$ ,  $\varepsilon_r = 0.6$ ,  $a_f = 5.0$ ,  
 $m = 1$ ,  $l = 0.5$ ,  $n = 1.0$ , Thickness of shear zone = 4 cm. The factor of plastic  
parameter is 3000.0.



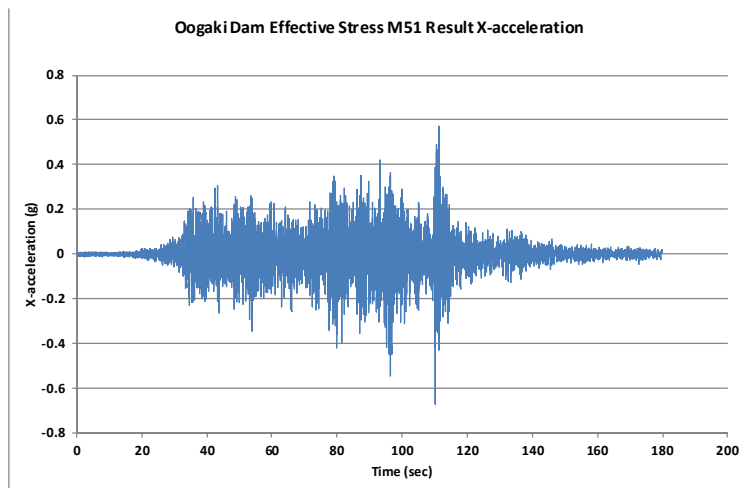
Computed crest acceleration by total  
stress analysis



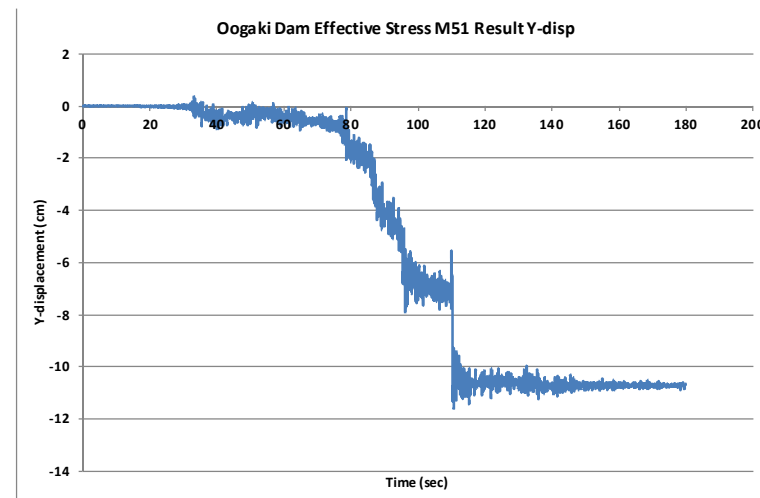
Computed crest settlement by total  
stress analysis

# DYNAMIC RESPONSE ANALYSIS BY KINEMATIC HARDENING ELASTO-PLASTIC MODEL (EFFECTIVE STRESS ANALYSIS)

$c = 11 \text{ kPa}$ ,  $\phi_p = 42.0^\circ$ ,  $\phi_r = 34.0^\circ$ ,  $\varepsilon_f = 0.03$ ,  $\varepsilon_r = 0.6$ ,  $a_f = 5.0$ ,  
 $m = 0.5$ ,  $n = 1.0$ , Thickness of shear zone = 4 cm.

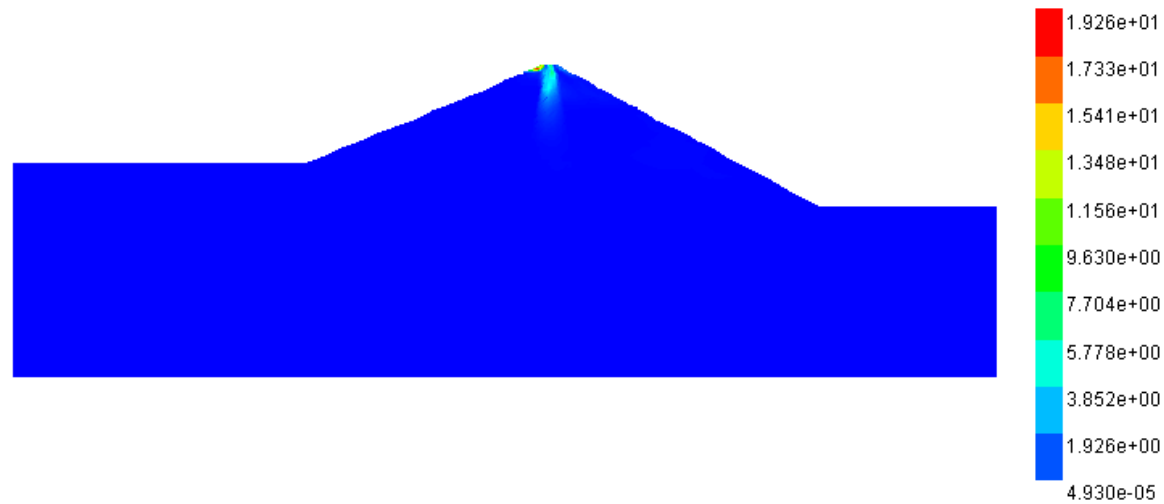


Computed crest acceleration by  
effective stress analysis



Computed crest settlement by  
effective stress analysis

# COMPUTED MAXIMUM SHEAR STRAIN (%) BY KINEMATIC HARDENING MODEL EFFECTIVE STRESS ANALYSIS



# SUMMARY

A dynamic progressive failure analysis of a small embankment dam using dry sand on shaking table is carried out. The acceleration simulating El Centro earthquake is applied to the base of shaking table. The computed acceleration at the crest of model dam is compared to the observed one and the computed displacement is also verified by the observed displacement. Then comparison of two and three dimensional analyses of dry sand embankment dam are also carried out.

A cumulative damage concept for simple elasto-plastic strain softening model is effective by using the results of cyclic triaxial tests of saturated soils. A shear banding constitutive model incorporating a characteristics length of shear band is also necessary. Both a simple strain softening constitutive model and a kinematic hardening model are also applicable to total stress dynamic response analyses by applying incompressible condition in case of saturated soils.

The computation of real fill-type dam is also carried out by total stress elasto-plastic constitutive model and effective stress constitutive model by taking into account the pore water build-up.

THANK YOU FOR  
YOUR ATTENTION

